



## Existe Realmente la Materia Oscura?

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“We habitually act upon hypotheses, but not precisely as we act upon what we consider certainties; for when we act upon an hypothesis we keep our eyes open for fresh evidence”

-Bertrand Russel-

“The difficulty lies not  
in the new ideas, but  
in escaping from the  
old ones”

-John Maynard Keynes-

## Spiral Rotation Curves



Surface density mass distribution follows  $\Sigma(r) = \Sigma_0 e^{-R}$ ,

with  $R = r/r_s$ .

Integral Mass distribution hence given by:  $M_D(< R) = M_D [1 - e^{-R} (R + 1)]$

Mass converges rapidly, over 90% within  $R = 4$  yet, rotation curves remain flat always at  $V(R) = V_{\text{inf}}$ , out to last measured point, sometimes  $R > 25$ .

No Keplerian fall off has ever been measured! end up with  $M_{\text{Tot}} \sim 20M_D$

$V_{\text{inf}}$  and  $r_s$  range from 10-300 km/s and 0.2-5 kpc.



## Galaxy cluster dynamics



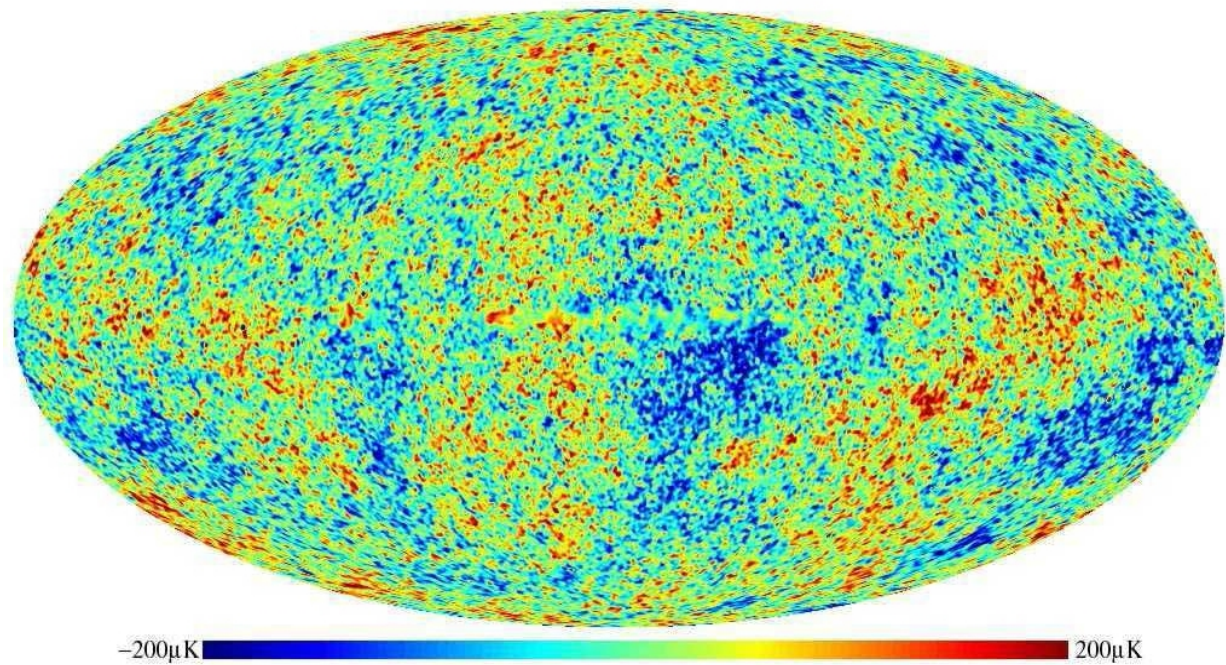
Radial Velocity of each individual galaxy measured, giving a velocity dispersion for the cluster,  $\sigma$

Total size (or half-light radius,  $R_{hl}$ ), hence yields total cluster mass  $M_C$  from virial equilibrium,  $2T + W = 0$ :

$$M_C \sigma^2 = \frac{GM_C^2}{0.5R_{hl}}$$

End up again with  $M_{Tot} \sim 20M_{Vis}$

## Structure Formation



Linearised expansion law, fluctuations grow as  $\delta\rho \propto (1+z)^{-1}$

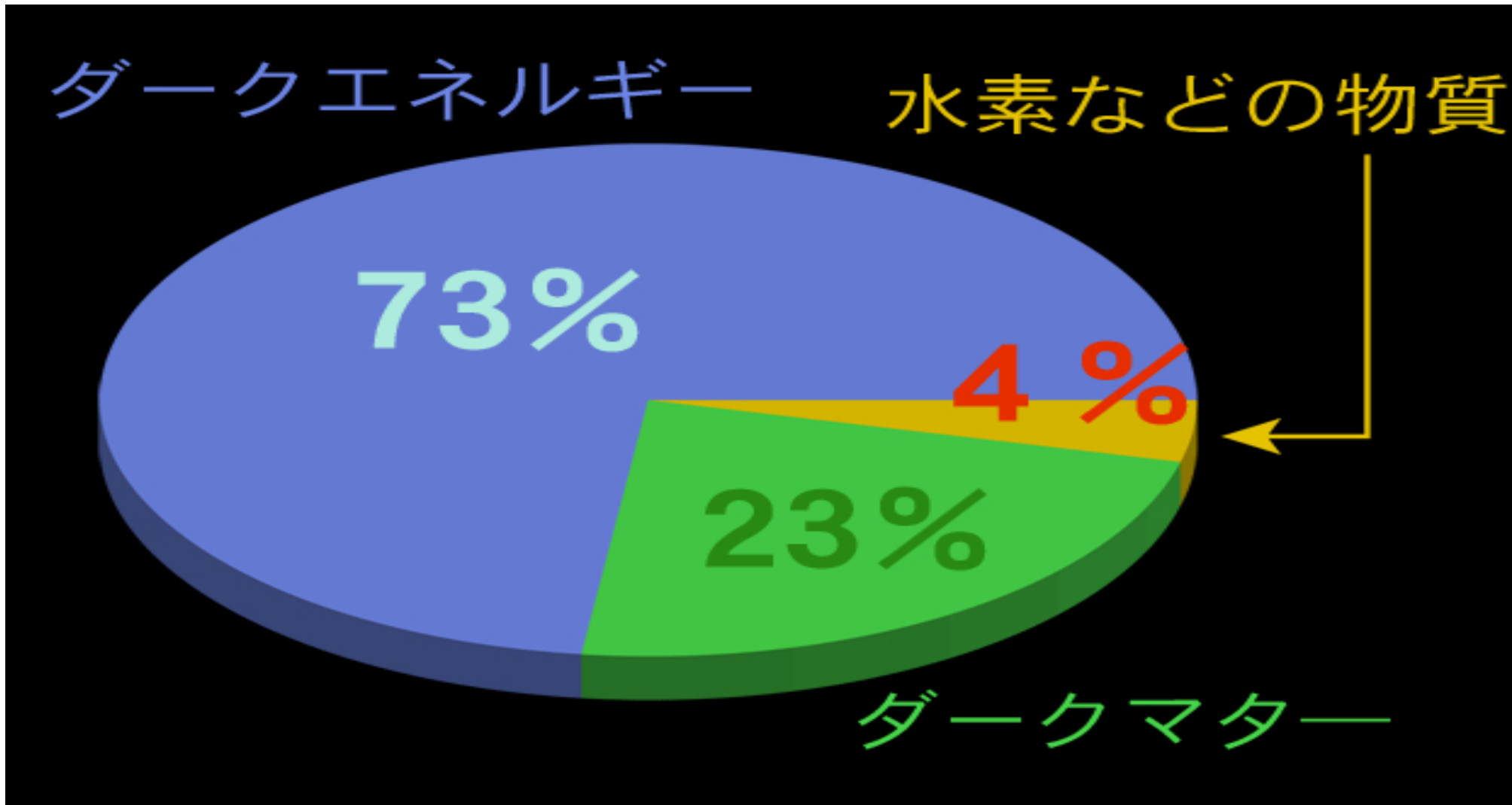
Since  $\gamma$  field energy density scales with  $\rho_\gamma \propto (1+z)^4$  and  $\rho_\gamma$  scales with  $T_\gamma^4$ ,  
Temperature scales with  $(1+z)$

Therefore, present temperature of 2.7K and 13.6 eV H ionisation potential  $\Rightarrow$  CMB emitted at  $z=1000$ .

Since  $\delta T$  (and hence  $\delta\rho$ ) only of 1 part in  $10^{4-5}$ , we should still be in the linear regime!

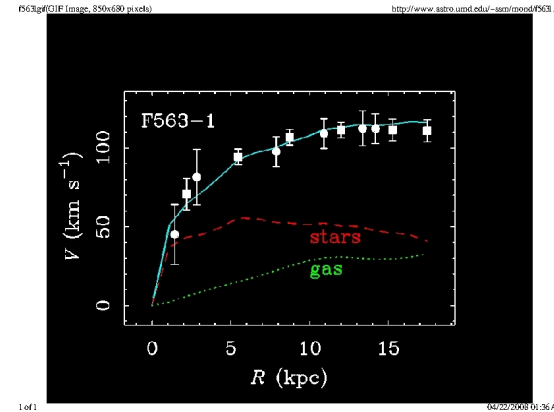
Need to boost gravity effect again, e.g.  $M_{Tot} \sim 20M_{Vis}$

Entonces de que esta hecho el Universo?

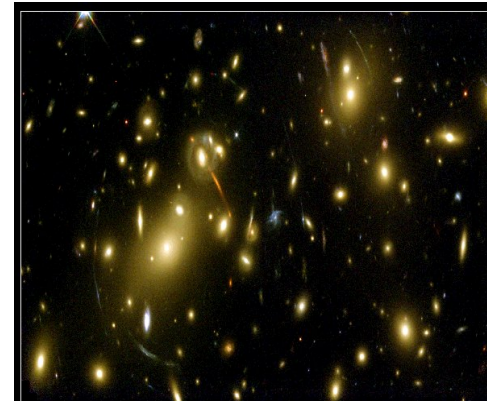


# Indirect evidence for Dark Matter?

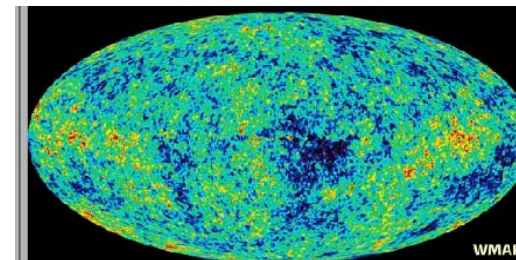
Rotation Curves of Large Spirals  
(1-10 kpc)



Dynamics and Lensing of Galaxy Clusters  
(1-5 Mpc)



Cosmological Matter Determinations  
( $> 50$  Mpc)



...or direct evidence for the failure of standard Gravity at large scales?

-Direct proof of the law of Gravity exists only for  $R < 0.001pc$

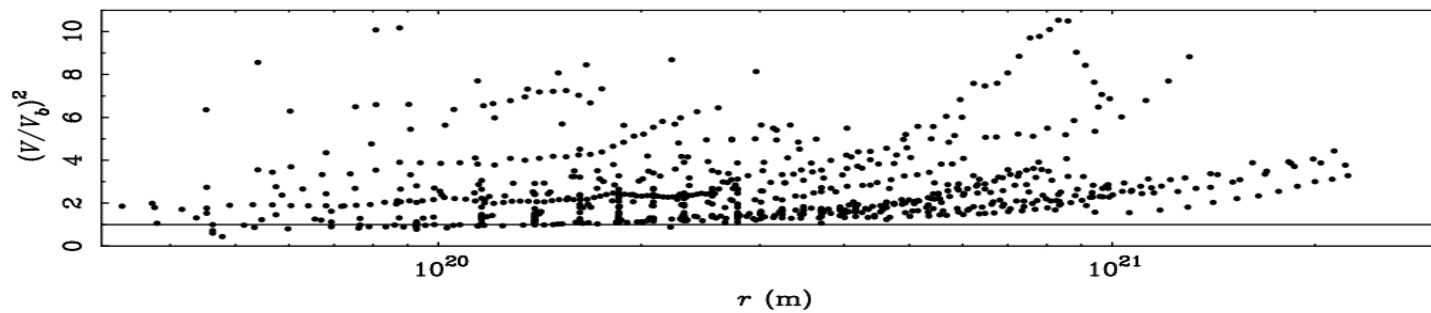
-Direct proof of the existence of Dark Matter is still missing





## Detailed Dynamics of Disk Galaxies

“Dark matter fraction” does not show any clear correlation with integral or differential Galactic properties.

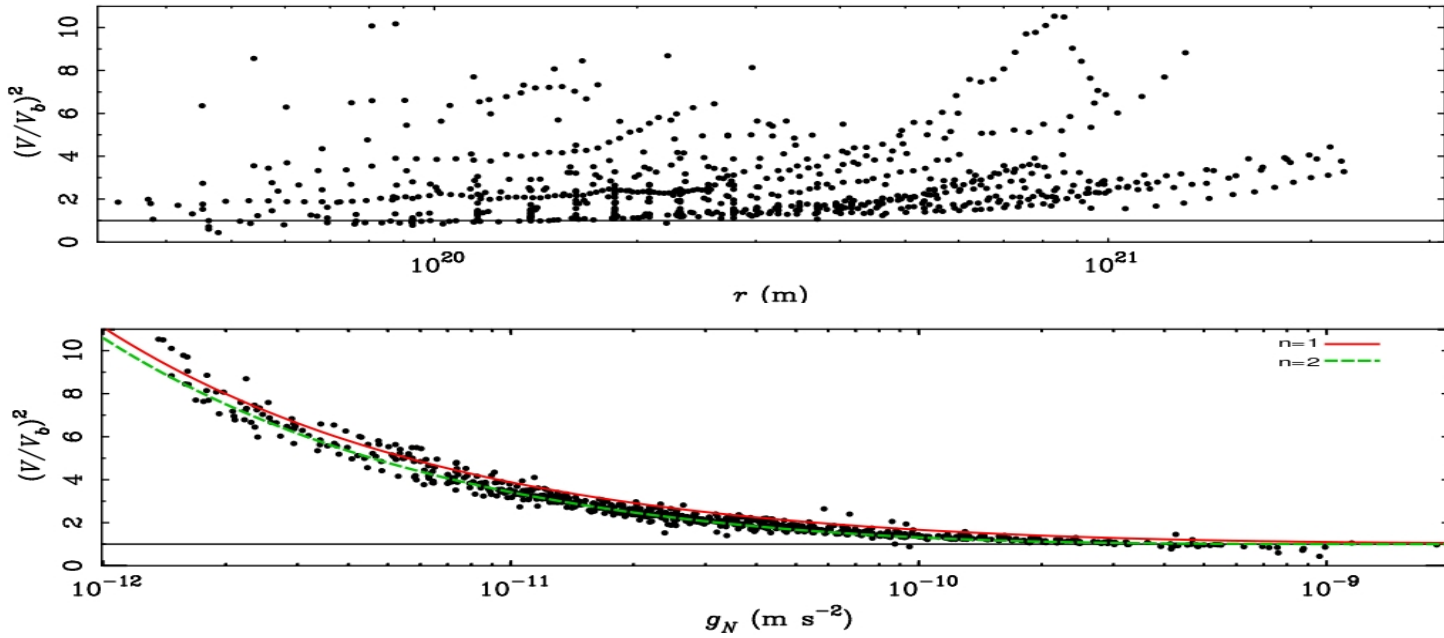




## Detailed Dynamics of Disk Galaxies

“Dark matter fraction” does not show any clear correlation with integral or differential Galactic properties.

However, mass discrepancy tightly correlates with acceleration, at all radii, for all galactic types.



Distribution of baryonic mass uniquely determines total rotation!

What would Newton have done?



Since  $F = ma$ , and for centrifugal equilibrium orbits  $a = V^2/r$ ,

Given the Solar System rotation curve  $V = \left(\frac{GM}{r}\right)^{1/2}$ ,

Gravitational force per unit mass is inferred to be:  $\frac{GM}{r^2}$ .

Take now the empirical rotation curves of galaxies,  $V = (GMa_0)^{1/4}$ ,

Gravitational force per unit mass is inferred to be:  $\frac{(GMa_0)^{1/2}}{r}$ .

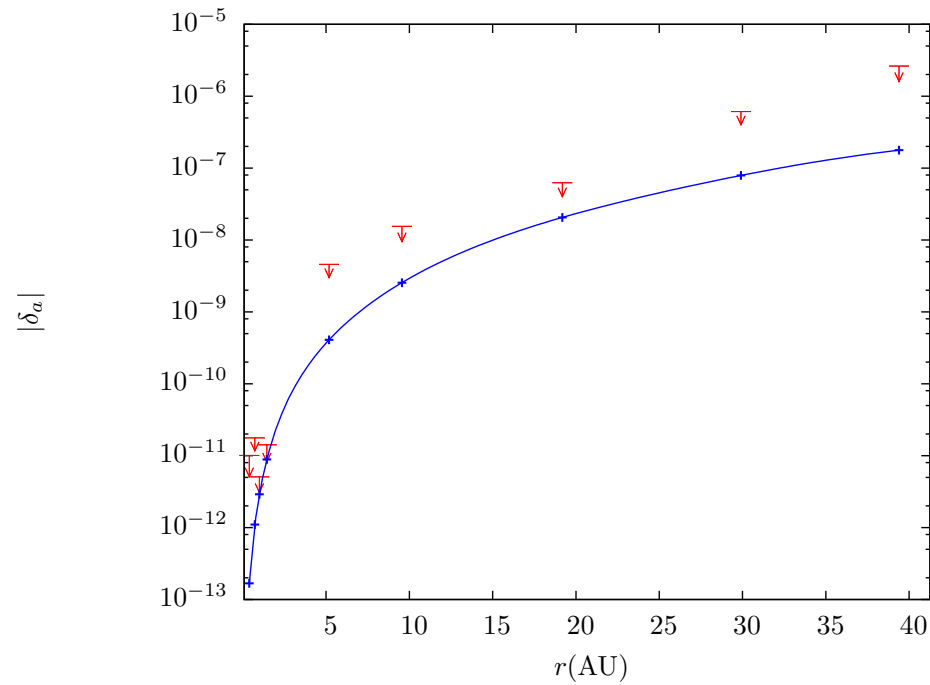
We can therefore write the dimensionless force per unit mass  $F/a_0$  as:

$$\frac{F_N}{a_0} = \left(\frac{GM}{a_0}\right) \frac{1}{r^2} \quad \frac{F_M}{a_0} = \left(\frac{GM}{a_0}\right)^{1/2} \frac{1}{r}$$

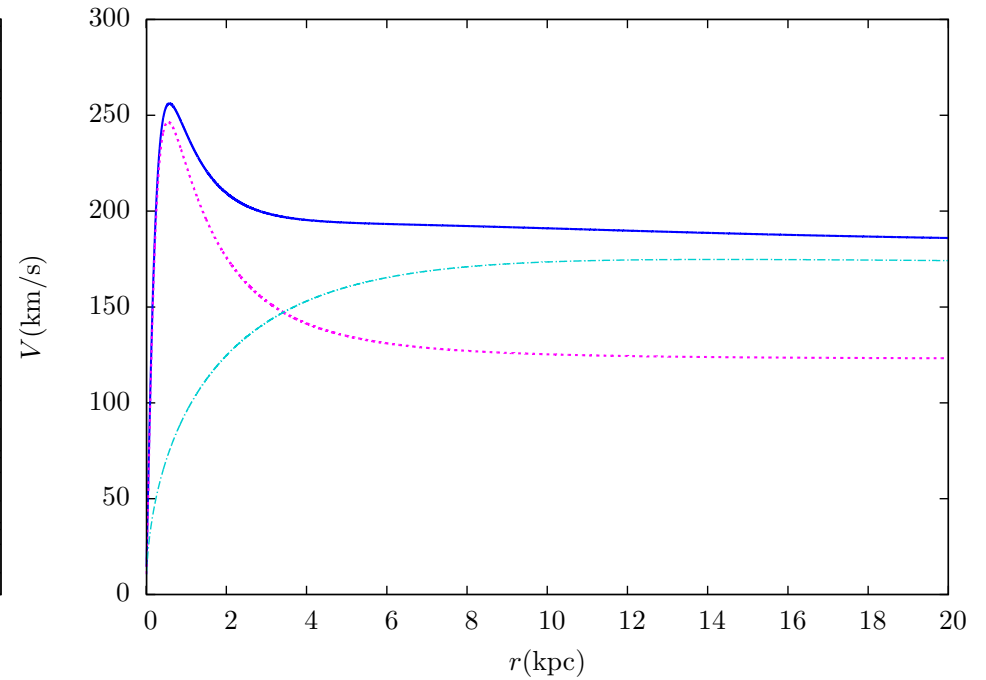
choosing  $x = \left(\frac{GM}{a_0}\right)^{1/2} \frac{1}{r}$  gives:

$$\frac{F_N}{a_0} = x^2 \quad \frac{F_M}{a_0} = x \quad \text{Perhaps } \frac{F}{a_0} = \dots + x^2 + x + \dots ?$$

# Self-consistency across astrophysical scales



Solar System.



Milky Way.







## Generic modified gravity predictions

1) All  $a > a_0$  systems in the low velocity regime should appear as purely Newtonian, without requiring any dark matter.

-Indeed, no counterexamples to this prediction exist.

2) All  $a < a_0$  systems in the low velocity regime should appear as purely “MONDian”, requiring substantial dark matter if interpreted under Newtonian Gravity.

-All known “dark matter” presenting systems neatly fall into this category.

-A definitive prediction appears for the outskirts of globular clusters and wide binaries

3) In the  $a < a_0$  regime, equilibrium velocities become flat, with systems exhibiting a

“Tully-Fisher” relation for  $V_{MG}^2 \propto (MGa_0)^{1/2}$

## Wide binaries as a critical experiment for gravity

A test particle orbiting a  $1M_{\odot}$  star in a circular orbit of radius  $s$ , will have an acceleration that falls below  $a_0 = 1.2 \times 10^{-10} m/s$  for:

$$s > 7000AU = 3.4 \times 10^{-2} pc .$$

Therefore, relative velocities of binaries wider than  $7000AU$  are predicted to be qualitatively and quantitatively very different under Newtonian Gravity and generically under modified gravity theories.

Which scaling will wide binaries show?

$$\Delta V_N = 2 \left( \frac{GM}{s} \right)^{1/2} \quad \text{or} \quad \Delta V_{MG} = 2(Ga_0M)^{1/4} ?$$

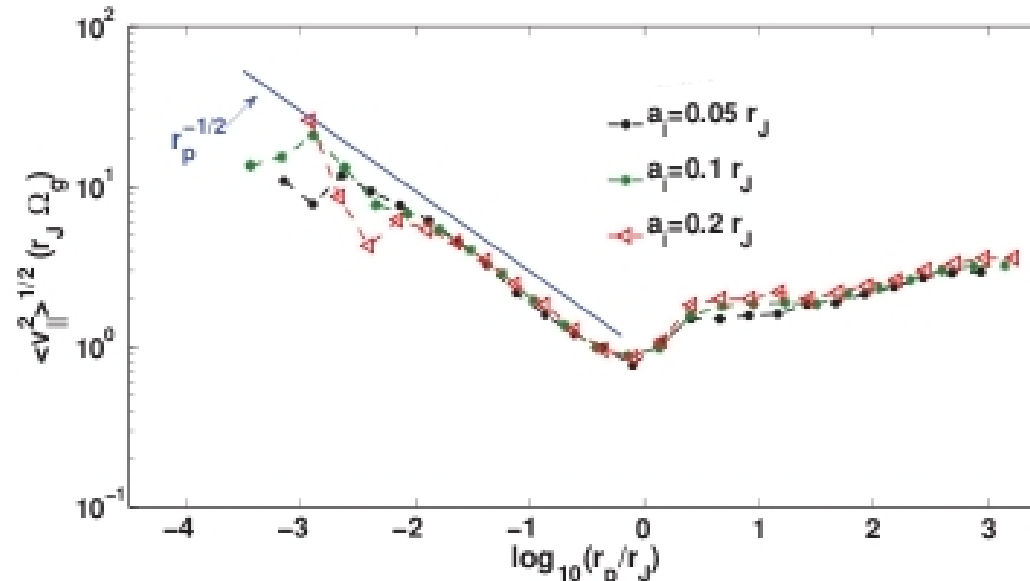
A large survey of relative proper motions and separations for wide binaries should yield a conclusive answer.



# Newtonian prediction for wide binary samples



Predicted projected RMS 1D  $\Delta V$  vs.  $s$  relation.



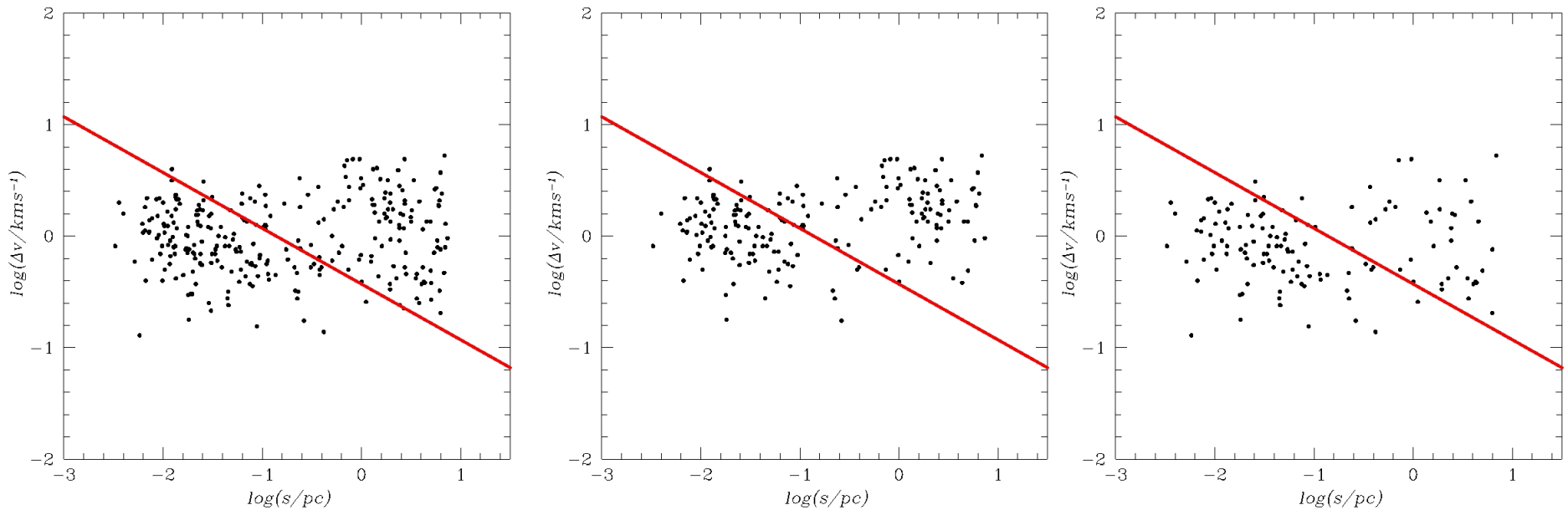
**Figure 7.** RMS line-of-sight relative velocity of the binaries as a function of projected separation, at the end of the simulations. The horizontal axis is the projected separation normal to a randomly chosen line of sight, while the vertical axis is the rms line-of-sight relative velocity in each separation. For Keplerian motion we expect  $\langle v_{||}^2 \rangle^{1/2} \propto r_p^{-1/2}$ , shown by the straight line. The relation between the line-of-sight relative velocity and the projected separation deviates from the Keplerian relation for  $r_p \gtrsim r_J$ .

- Below  $s = r_J = 1.7pc$ , curve closely follows Kepler's law.
- Mostly, disruption occurs for  $s > r_J$ , the tidal radius of the problem.  
 $\Rightarrow$  a definitive feature expected at  $s = r_J = 1.7pc$
- Unbound stars continue to drift along very similar orbits and will show up in observational samples.

## Wide binary catalogues -2) *Hipparcos*



From a catalogue of  $\sim 280$  carefully selected wide binaries we obtain relative velocities on the plane of the sky and projected separations, average S/N=2.0.



- The upper envelope clearly defines a **horizontal line**, showing the “flat rotation curve” of modified gravity, and **not the Keplerian decline** of Newtonian gravity.

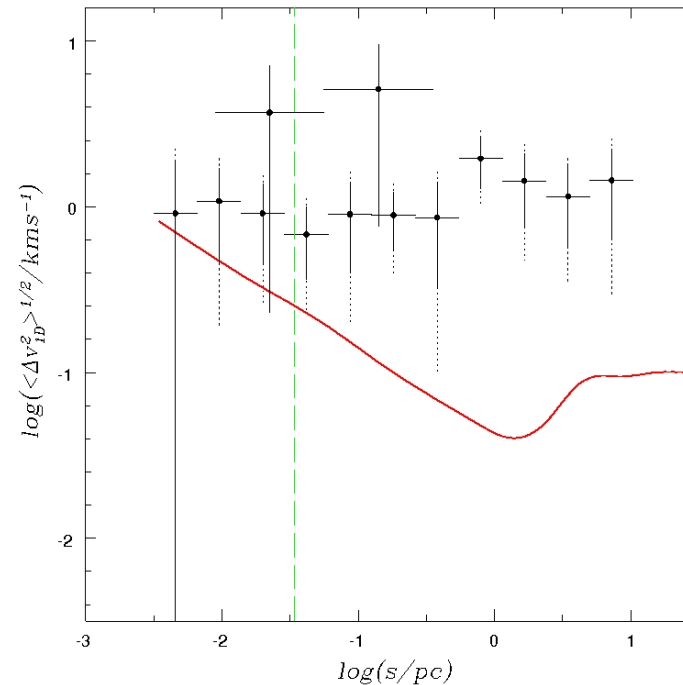
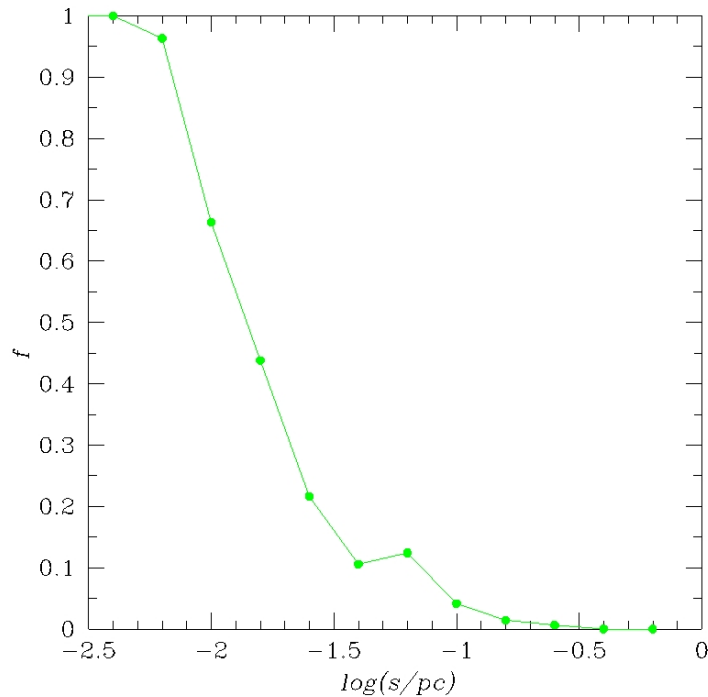
- It can be shown that results are not driven by errors or catalogue selection cuts.

-The data show **no feature** of any kind on crossing the Newtonian tidal radius at 1.7pc.

## Wide Binary conclusions

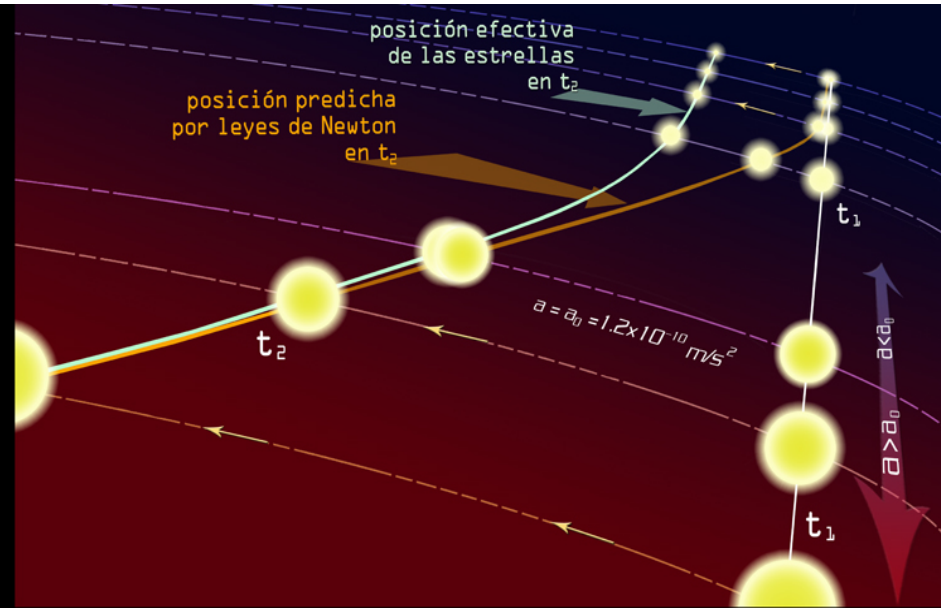
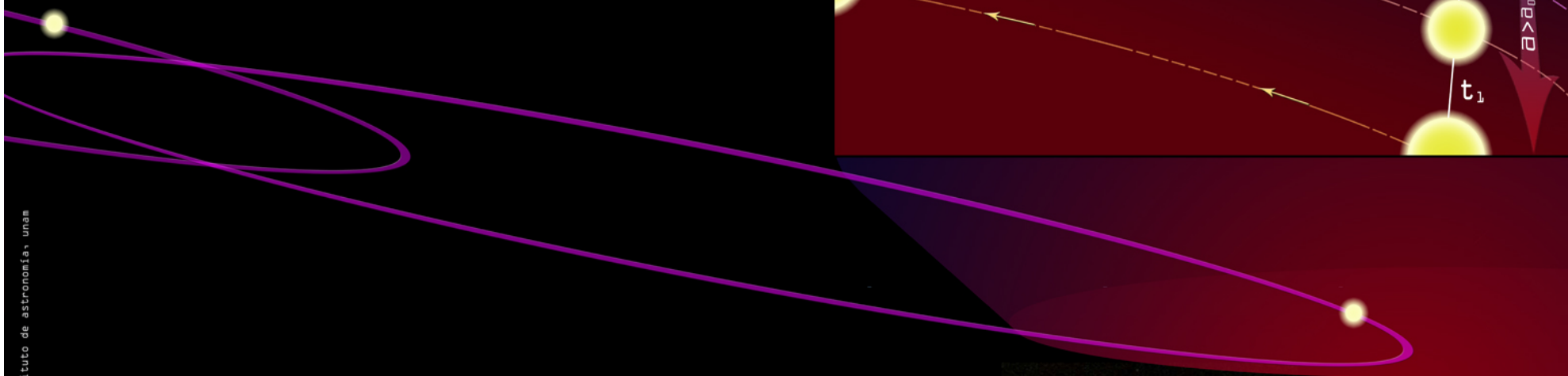


Quantitative comparison with full Newtonian prediction:



- The trends shown by the data are clearly defining the **modified gravity phenomenology**, Newtonian Gravity is only consistent with the data with a probability  $< 3 \times 10^{-5}$ .
- The two completely independent catalogues yield **fully consistent results**.
- The data rule out the Newtonian model at a  **$4\sigma$**  level.

# movimiento de las estrellas binarias extendidas



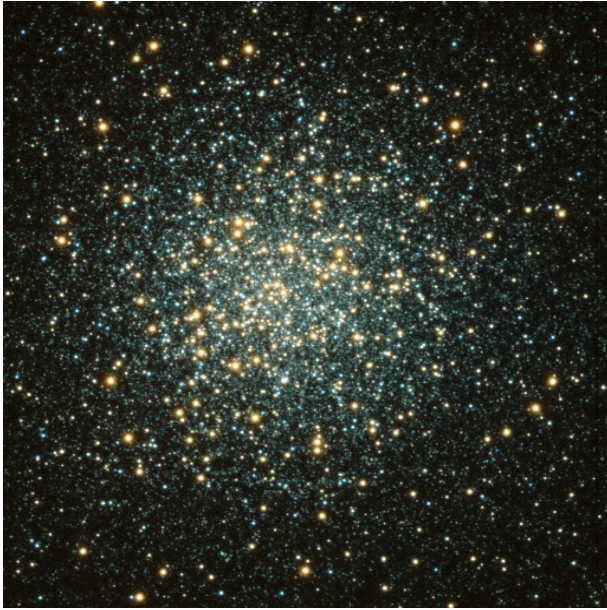
diseño: mariana espinosa aldama, instituto de astronomía, unam



El desplazamiento de las estrellas binarias separadas por más de 1000 UA no coincide con el predicho por la Ley Universal de Gravitación de Newton. La discrepancia se observa a partir del punto en que la aceleración sufrida por las estrellas es menor a la aceleración de Milgrom ( $a_0$ ). La velocidad orbital de las binarias extendidas se vuelve constante a partir de  $a_0$ . La fuerza deja de ser inversamente proporcional a  $r^2$  y comienza a ser inversamente proporcional a  $r$ , confirmando la predicción de la teoría de Gravitación Extendida.



## Surprising New GC Results:



Total masses  $\sim 10^5 - 10^6 M_{\odot}$

Half mass radii  $\sim 20 pc$

Up to now, with stellar velocity dispersion profiles measured towards the **core regions**, well modelled as **purely Newtonian** equilibrium structures, without any Dark Matter.

# The outskirts of GCs



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## Testing Newtonian gravity with distant globular clusters: NGC1851 and NGC1904\*

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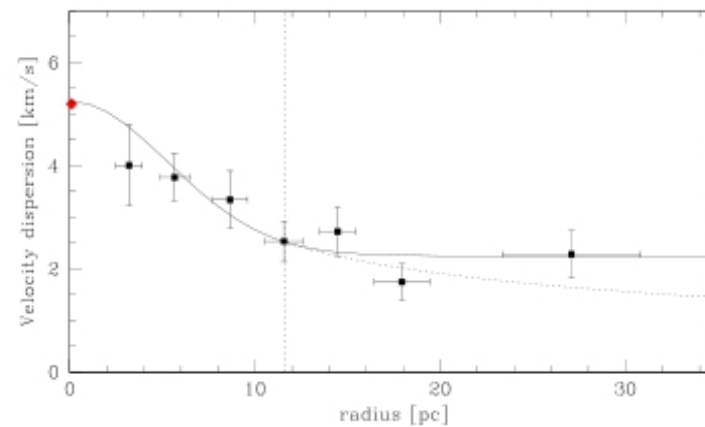
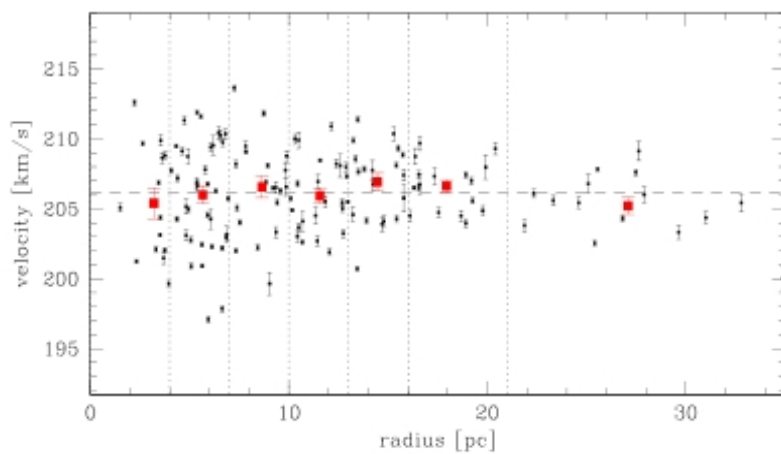
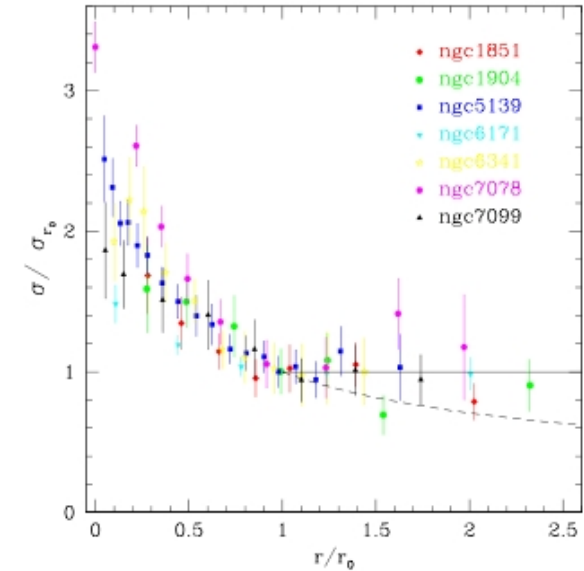
<sup>1</sup> Instituto de Astrofísica de Canarias, Spain

<sup>2</sup> European Southern Observatory, Chile

<sup>3</sup> Osservatorio Astronomico di Padova, Italy

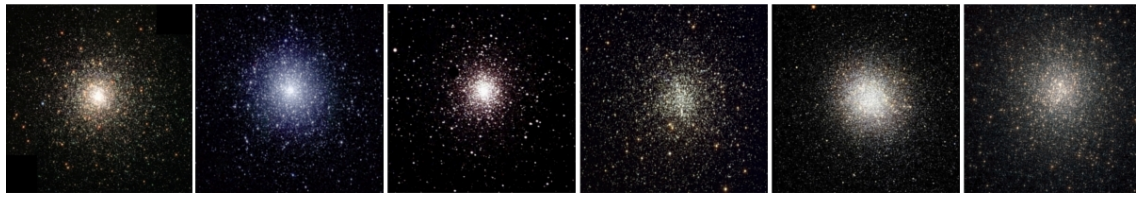
<sup>4</sup> Universidad de Concepcion, Departamento de Astronomia, Concepcion, Chile

August 23, 2010





## The outskirts of GCs

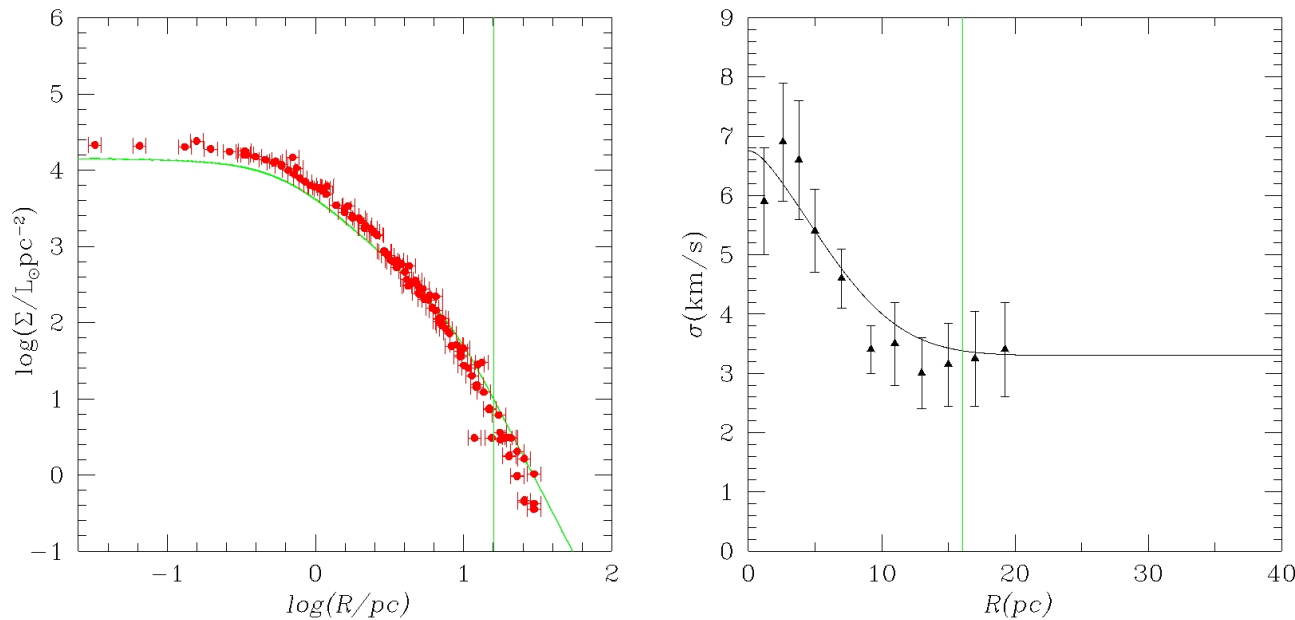


Using the modified force model, we solve equation:

$$\sigma(r) \frac{d\sigma(r)}{dr} + \sigma(r)^2 \left[ \left( \frac{dM}{dr} \right)^{-1} \frac{d^2 M}{dr^2} - \frac{2}{r} \right] = F (GM(r)/a_0 r^2)$$

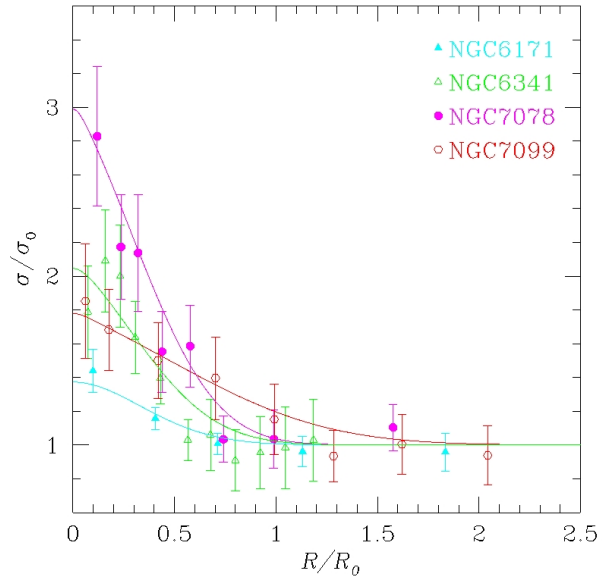
with  $F(X) = X \left( \frac{1-X^{10}}{1-X^9} \right)$

Constrained to give measured total mass, half mass radius, central stellar volume density and observed projected velocity dispersion and brightness profiles. Model for NGC 6341.



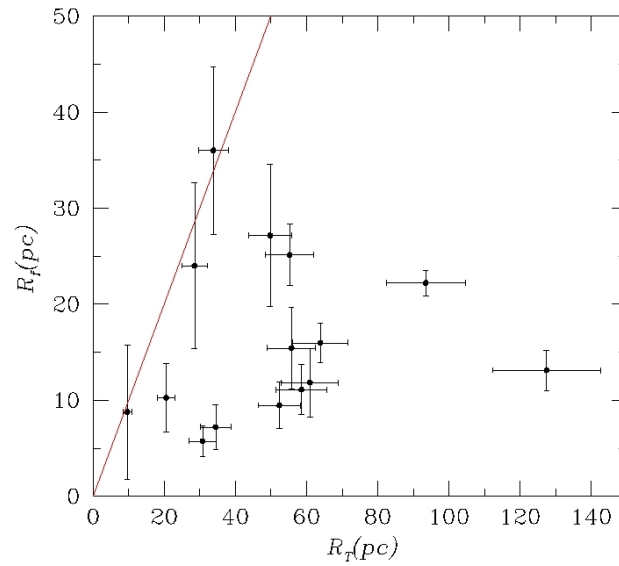
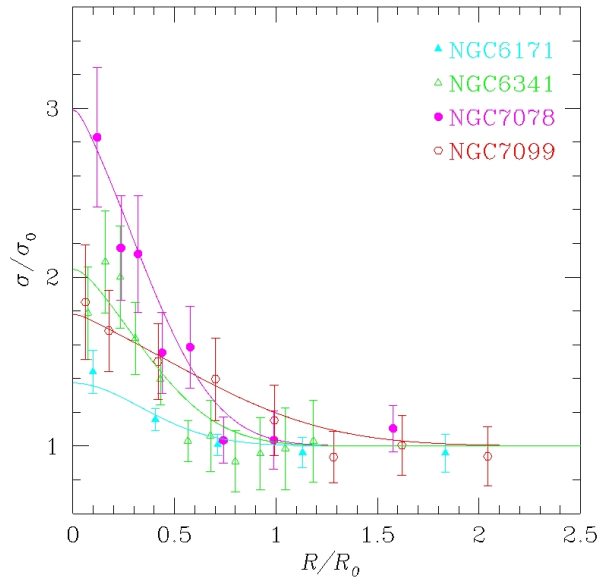
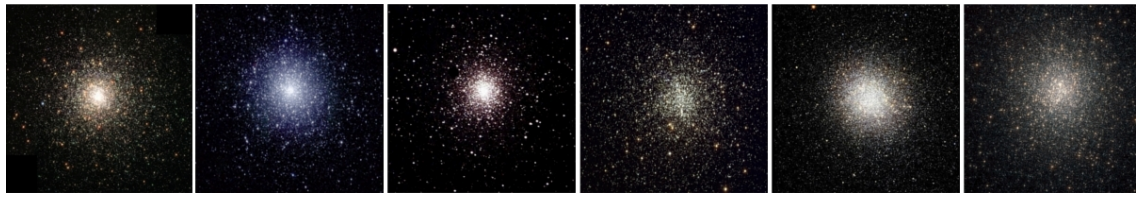
All observational parameters are fitted simultaneously. Vertical line gives point at which  $X = 1$

## GC conclusions



Flattening of the velocity dispersion profile closely coincides with  $a = a_0$  threshold

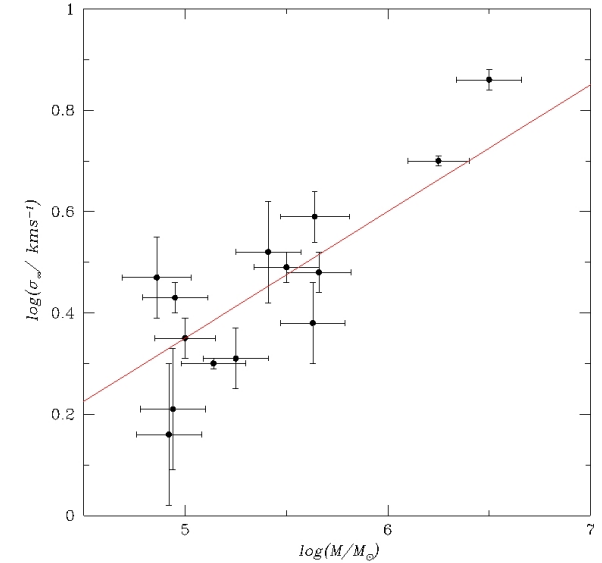
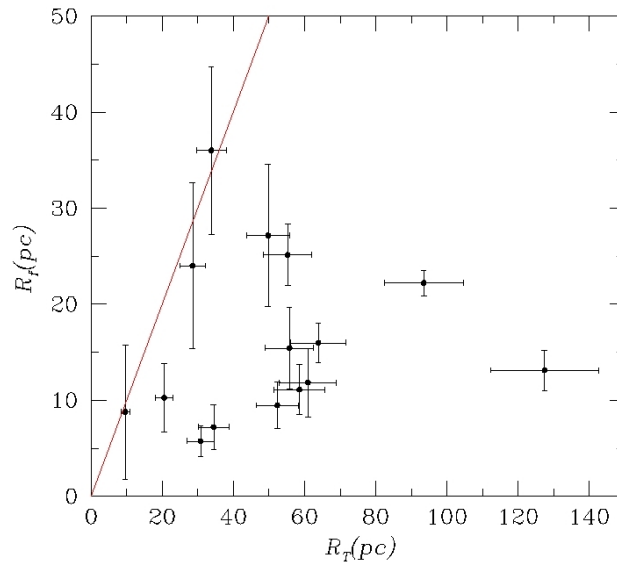
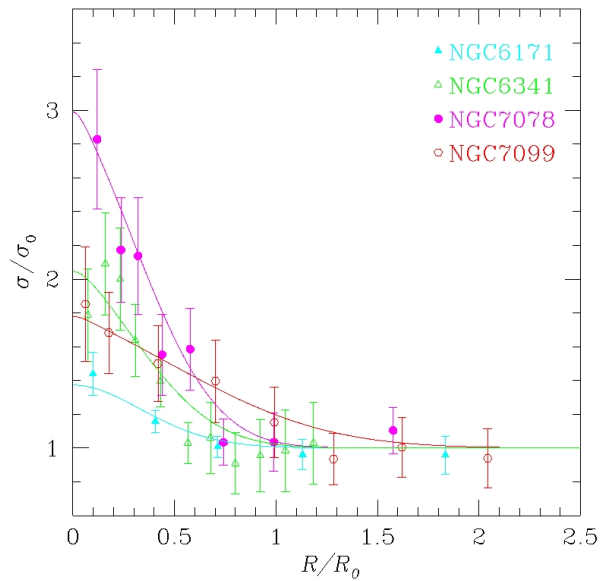
## GC conclusions



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Using total masses from detailed stellar population modelling tuned to each individual GC, Even at perigalacticon, all the GC in the sample are smaller than their Newtonian tidal radii.

## GC conclusions



Flattening of the velocity dispersion profile closely coincides with  $a = a_0$  threshold

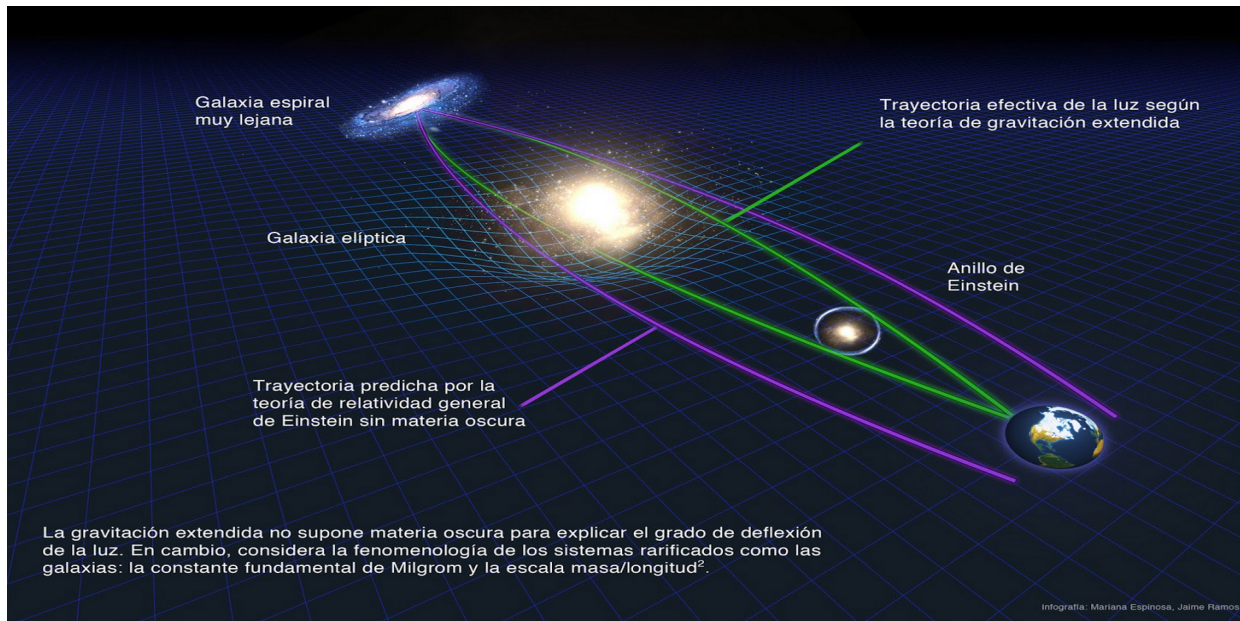
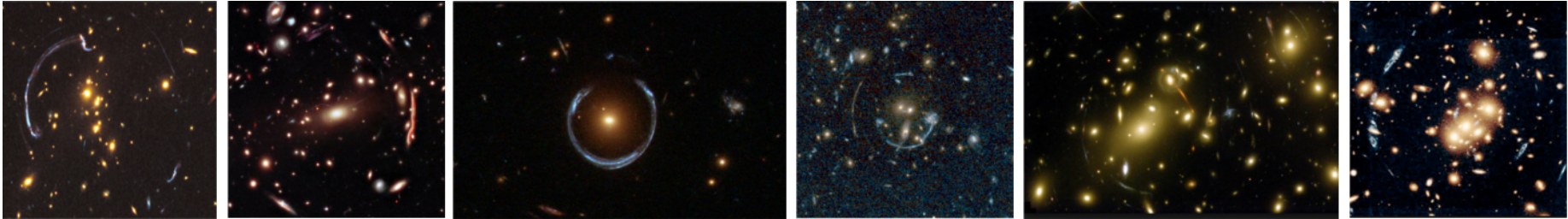
Using total masses from detailed stellar population modelling tuned to each individual GC, Even at perigalacticon, all the GC in the sample are smaller than their Newtonian tidal radii.

Fractional fall in  $\sigma$  correlates with fraction of the GC within  $a < a_0$ .

$\sigma$  vs. Mass relation compatible with expected “Tully-Fisher”  $a_0$  relation.



# Lentes Gravitacionales como Experimento Crítico



- Mientras que las órbitas de partículas con masa (e.g. estrellas) dependen solo de las distorsiones en el paso del tiempo como función de la posición, las trayectorias de rayos de luz dependen también de las distorsiones en la medida del espacio como función de la posición.
- Presentamos la única teoría a la fecha de gravedad modificada que explica tanto los movimientos estelares como la deflexión de la luz, sin requerir nada de materia oscura.

What about the bullet cluster?

.

Originally touted as a proof of the existence of dark matter

What does it really show?



X-ray/Optical Composite of 1E 0657-56

...merely that the gas has been subject to classical hydrodynamical effects, showing the encounter to have been strongly supersonic, and that the gravitational signal is centred not on the diffuse gas, but on the 'point like' baryonic galaxies ...

.

What about the bullet cluster?

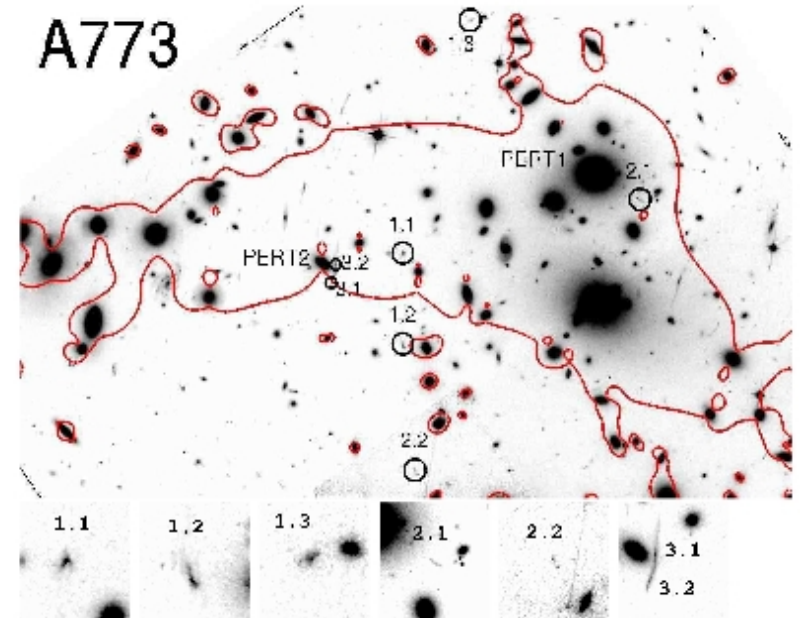
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Originally touted as proof of the existence of dark matter

What does it really show?



X-ray/Optical Composite of 1E 0657-56



...as would be expected in any normal or modified gravity model.

To first order, the observation is compatible under both points of view, ...only to first order!

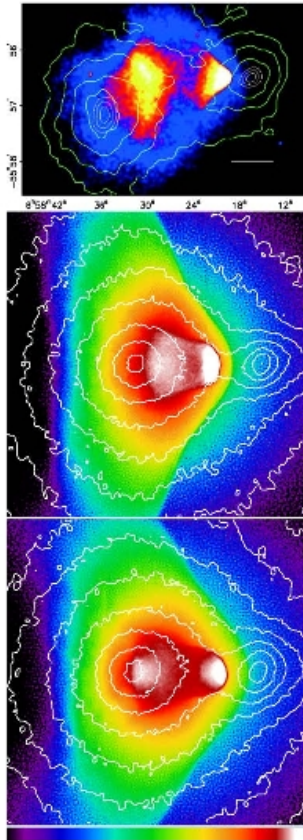
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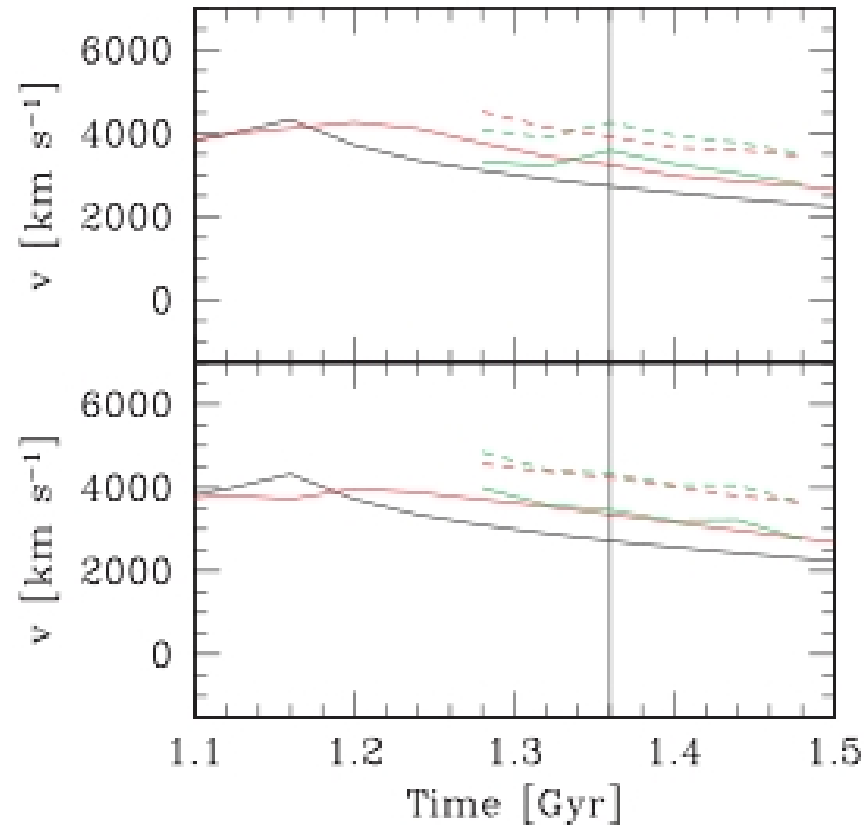
# What about the bullet cluster?

Detailed hydrodynamical modelling has shown the encounter velocity to have been  $> 3500 \text{ km/s}$ , significantly larger than the escape velocity of the cluster!

970 *C. Mastropietro and A. Burkert*



**Figure 1.** Upper panel: 500-ks *Chandra* image of the system with weak lensing  $k$  reconstruction shown in green (courtesy of D. Clowe and reproduced by permission of the AAS). Central and bottom panels: 0.8–4 keV surface brightness maps of runs 6:v3000b0 and 6:v3000b0. Logarithmic colour scaling is indicated by the key at the bottom of the figure with violet corresponding to  $10^{20} \text{ ergs}^{-1} \text{ kpc}^{-2}$  and white to  $2 \times 10^{21} \text{ ergs}^{-1} \text{ kpc}^{-2}$ . White contours trace the total surface mass density of the system within  $2.3 \times 10^3$  and  $2.3 \times 10^3 M_{\odot} \text{ kpc}^{-2}$ . The box size is 1800 kpc.

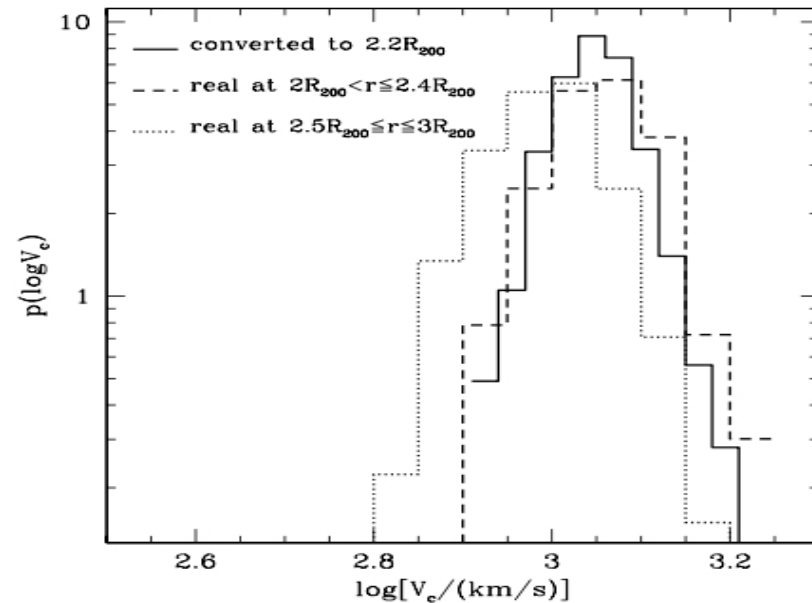


**Figure 16.** Run 10:1vb0c2 (top panel) and 10:1vb0c2nfw (bottom panel). Same as in Fig. 14.

This essentially rules out Classical gravity at this scale!



What about the bullet cluster?



**Figure 6.** Testing Equation (1). The dashed line shows the distribution of  $\log V_c$  in  $2 \leq r/R_{200} \leq 2.4$  measured from the simulation, while the solid line shows the distribution of  $\log V_c$  at  $r_{\text{in}} = 2.2R_{200}$  calculated from the measured distribution in  $2.5 \leq r_{\text{out}}/R_{200} \leq 3$  (dotted line) and Equation (1).



X-ray/Optical Composite of 1E 0657-56

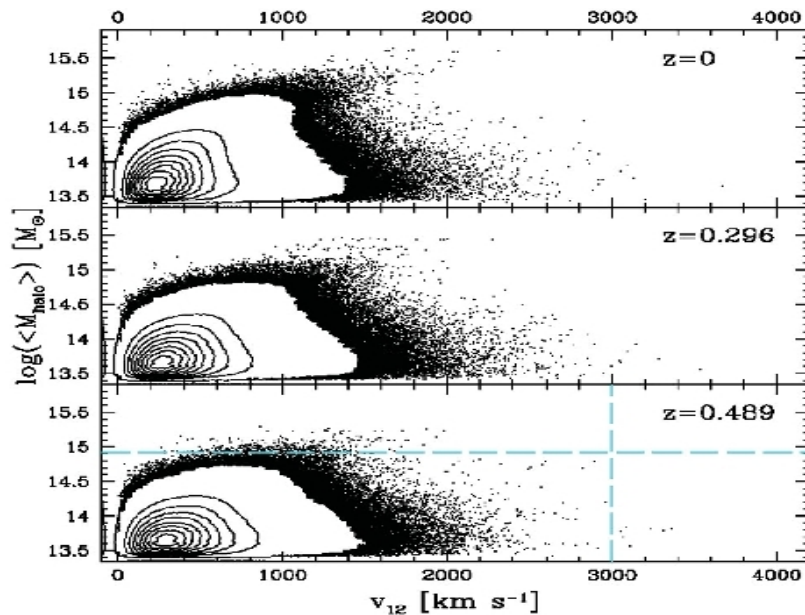
also has to be excluded because it cannot reproduce the observed X-ray brightness ratio of the main and subcluster or the X-ray morphology of the main cluster.

In this paper, we have shown that such a high velocity at 5 Mpc, which is about two times  $R_{200}$  of the main cluster, is incompatible with the prediction of a  $\Lambda$ CDM model. Using the results at  $z = 0$  and  $M_{\text{main}} \geq 0.7 \times 10^{15} h^{-1} M_{\odot}$ ,  $\Lambda$ CDM is excluded by more than 99.91% confidence level (none of the 1135 subclusters have  $V_c \geq 2000 \text{ km s}^{-1}$  in  $2 \leq r/R_{200} \leq 3$ ). For a lower minimum main cluster mass,  $M_{\text{main}} \geq 0.5 \times 10^{15} h^{-1} M_{\odot}$ ,  $\Lambda$ CDM is excluded by more than 99.95% confidence level (none of the 2189 subclusters have  $V_c \geq 2000 \text{ km s}^{-1}$  in  $2 \leq r/R_{200} \leq 3$ ).

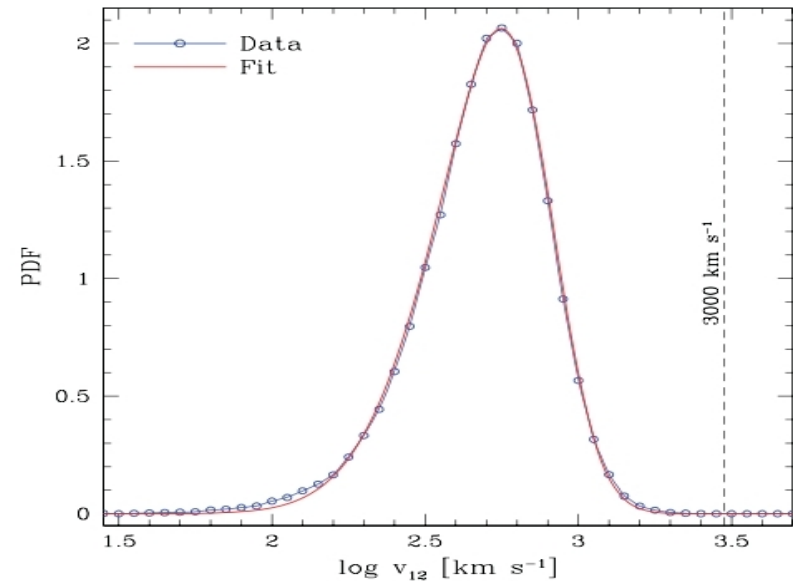
Encounter velocity necessary to obtain hydrodynamical signature is incompatible with classical gravity.

A recent independent confirmation

Detailed cosmological modelling has shown the encounter velocity to be outright incompatible with standard  $\Lambda$ CDM structure formation scenarios.



**Figure 13.** Average mass of halo pairs versus their pairwise velocity for the L2016N1008 run at  $z = 0.0, 0.296$  and  $0.489$ . In the bottom panel ( $z = 0.489$ ), the horizontal dashed line represents an average pair mass of  $8.25 \times 10^{14} M_{\odot}$  for 1E0657–56, and the vertical dashed line represents a pairwise velocity of  $3000 \text{ km s}^{-1}$  suggested by Mastropietro & Burkert (2008).



**Figure 15.** Pairwise velocity PDF for halo pairs with masses above  $10^{14} M_{\odot}$  in our L2016N1008 run. The blue circles represent  $v_{12}$  binned PDF data, the blue curve is the linearly interpolated values, and the red curve is the best-fitting skew normal distribution (Azzalini & Capitanio 2010). Integrating the fit from  $v_{12} = 3000 \text{ km s}^{-1}$  to infinity gives  $P(>3000 \text{ km s}^{-1}) = 2.8 \times 10^{-8}$ . This very low probability suggests that it is very difficult to produce a halo pair with high mass and high  $v_{12}$  as the observed 1E 0657–56.

This essentially rules out Classical gravity at this scale!

Understanding the impossibility of the bullet cluster under standard gravity

The sound speed for a gas in equilibrium with a dark halo having DM velocity dispersion  $\sigma$  is:  $c = \sigma$ .

The rotation velocity of this halo will be  $V_R = 2^{1/2}\sigma$ .

The escape velocity will therefore be  $V_e = 2^{1/2}V_R = 2c$ .

Releasing the “bullet” from infinity will therefore yield a maximum Mach number for the collision of  $V_e/c \Rightarrow$   $M_{max} = 2$

From looking at the picture it is evident the collision resulted in a strong shock with

$M_{obs} \approx 3$  or above.

Within a cosmological scenario, one has to start by overcoming the (accelerated!) expansion, which results in maximum Mach numbers even smaller than 2.

No amount of DM helps, as adding DM increases both  $V_e$  and  $c$  in the same proportion.

Under standard gravity it is impossible to produce Mach numbers as required to obtain the observed hydrodynamical signal, which explains the results of Lee & Komatsu (2010) and Thompson & Nagamine (2012).

## Understanding the bullet cluster under extended gravity

We can get the collision velocity to first order from:

$$F = \frac{(GMa_0)^{1/2}}{r} = \frac{dV}{dt} = \frac{dV}{dr}V$$

$$VdV = (GMa_0)^{1/2} \ln(r)$$

releasing the “bullet” from rest at a distance  $r_0$ , we see that V impact at  $r=5$  Mpc implies:

$$\frac{V^2}{2} = (GMa_0)^{1/2} \ln(r_0/5Mpc)$$

for a total baryonic mass of  $3 \times 10^{14}$ , obtaining V impact = 3,000 km/s requires:

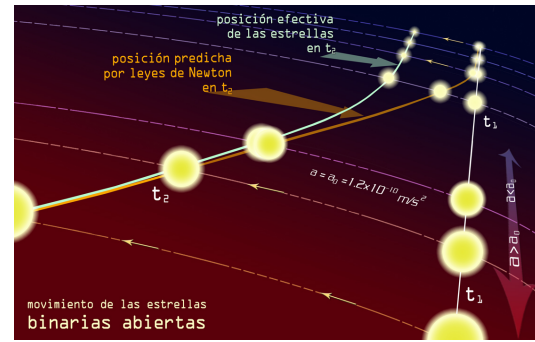
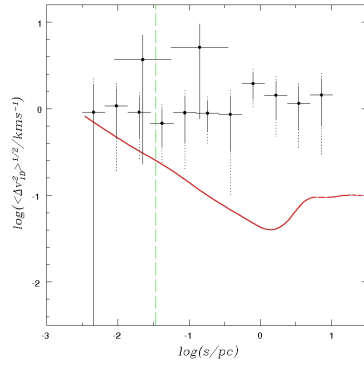
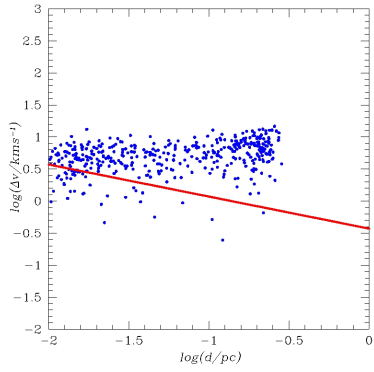
$$3000 = 0.5(3 \times 10^{14})^{1/4} [\ln(r_0/5Mpc)]^{1/2}$$

which yields,  $r_0 = 8.33 \times 5Mpc$ .

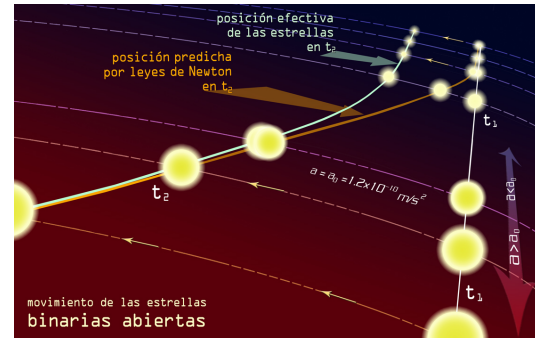
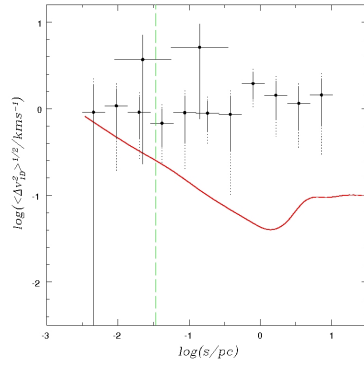
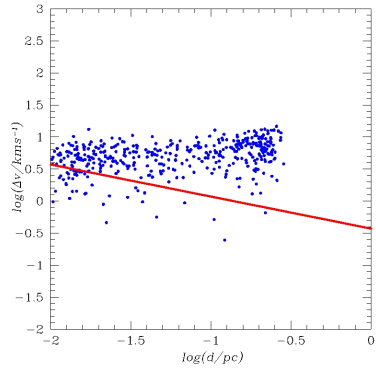
By comparison, the Newtonian escape velocity of the system, including hypothetical DM, at 5 Mpc is of only  $\sim 1,000$  km/s.

Under extended gravity schemes, starting from merely  $\sim 10$  times the observed size of the system, one can easily obtain impact velocities as required to obtain the observed hydrodynamical signal.

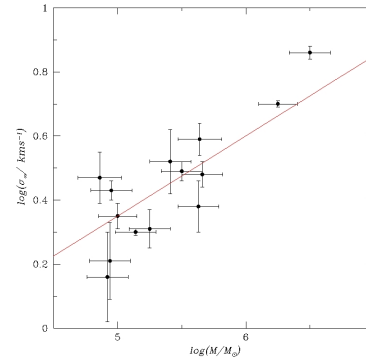
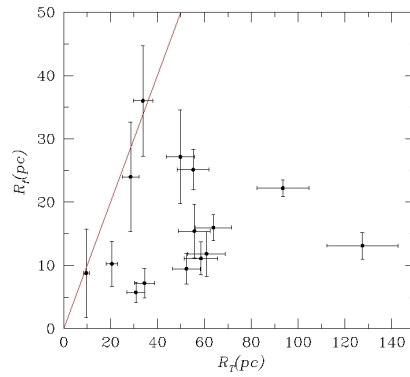
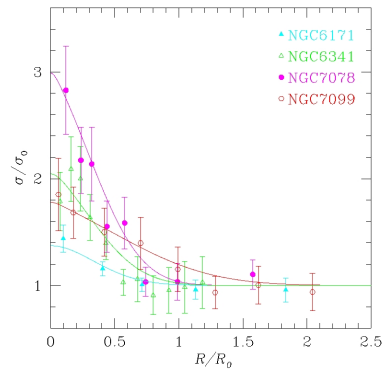
# The relative velocities of observed Wide binaries are inconsistent with Newtonian Gravity and GR



The relative velocities of observed Wide binaries are inconsistent with Newtonian Gravity and GR

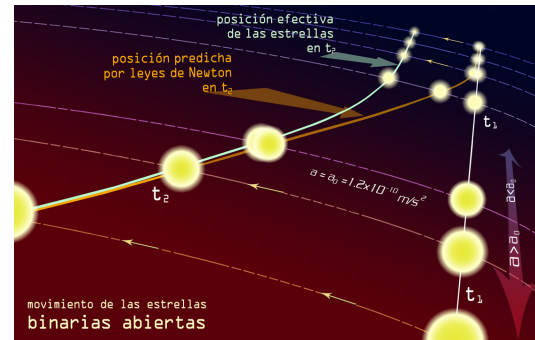
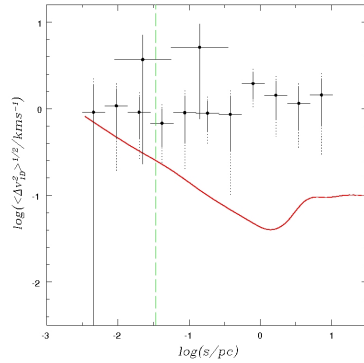
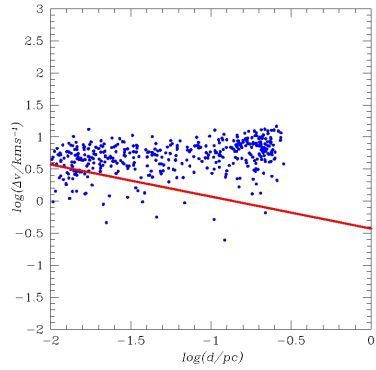


Outer velocity dispersions of globular clusters become flat and show the same galactic  $\sigma \propto M^{1/4}$  TF scaling

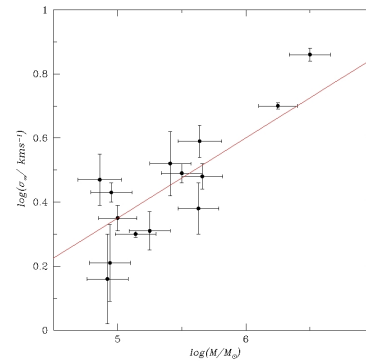
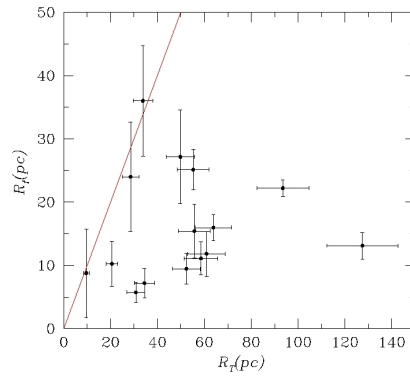
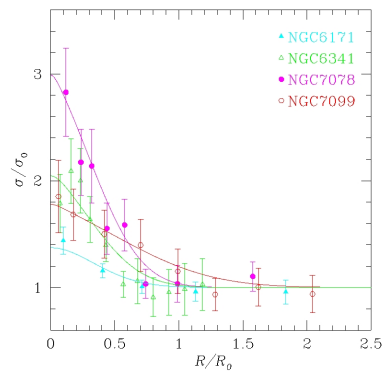
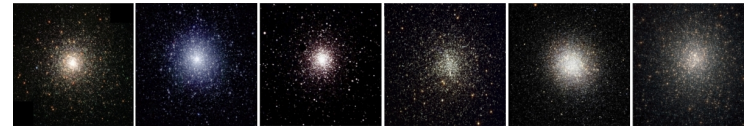




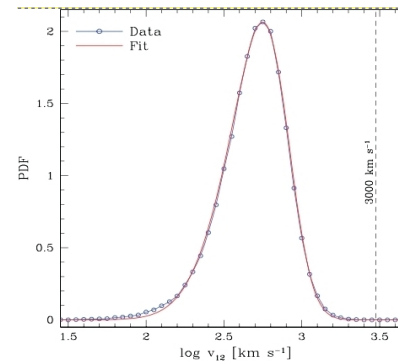
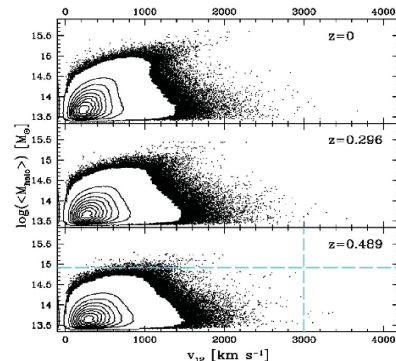
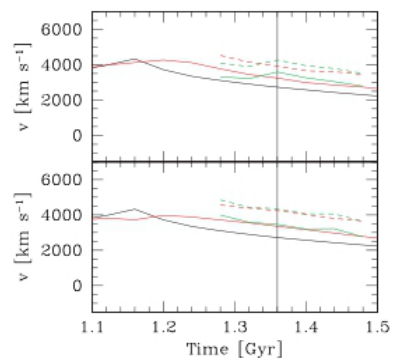
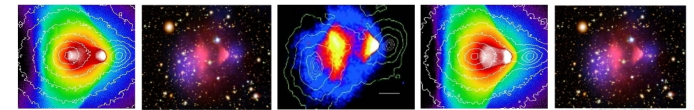
The relative velocities of observed Wide binaries are inconsistent with Newtonian Gravity and GR



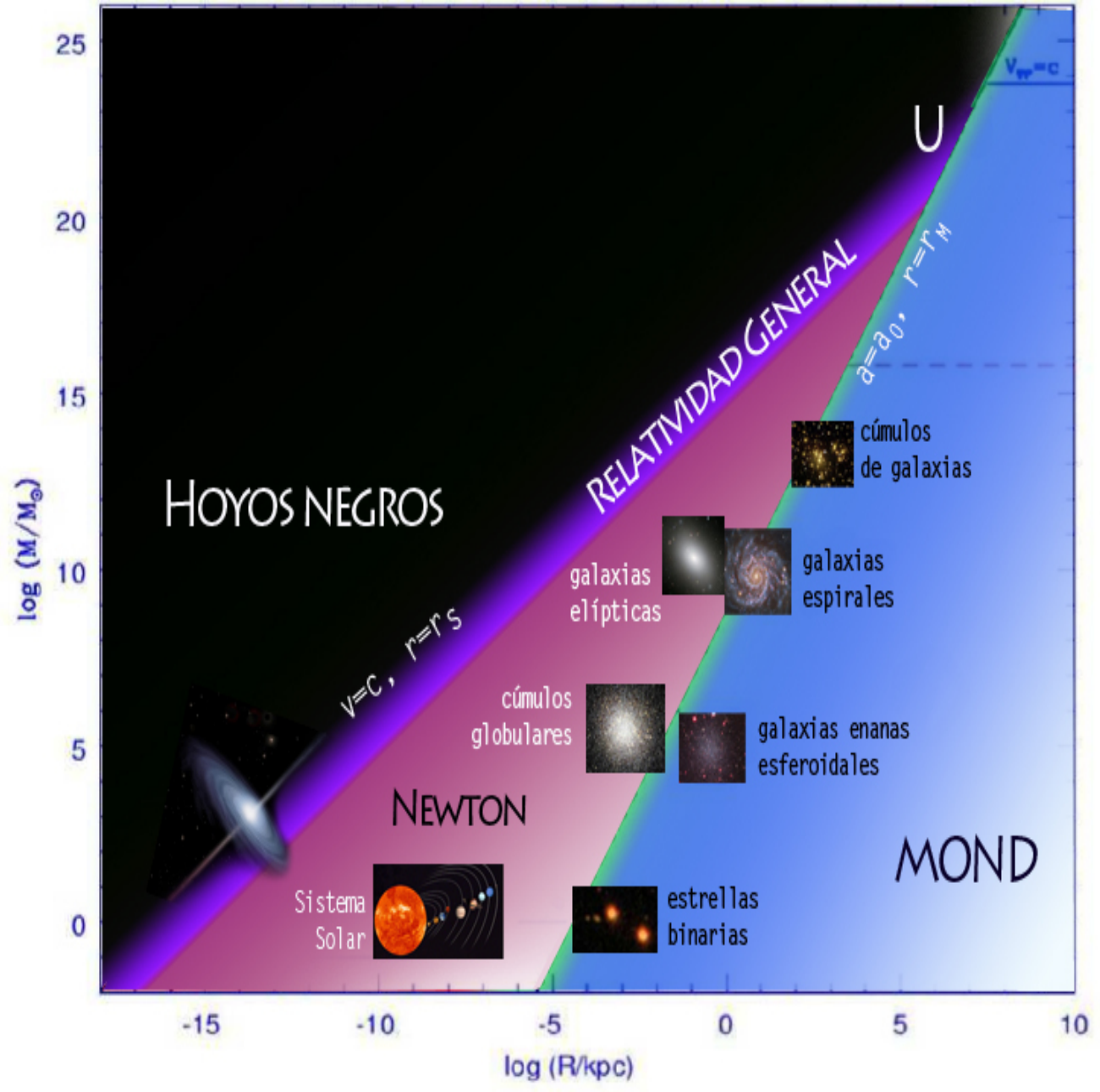
Outer velocity dispersions of globular clusters become flat and show the same galactic  $\sigma \propto M^{1/4}$  TF scaling



Infall velocity of the Bullet Cluster is larger than escape velocity, and hence incompatible with classical gravity



Overall scalings:





Conclusion:

The end of the validity regime  
for Newtonian gravity and GR  
has now been observed in a variety  
of low acceleration astrophysical systems.

### Mr. COTES'S PREFACE.

arise from the particular natures of those bodies. But whence it is that bodies derive those natures they don't tell us; and therefore they tell us nothing. And being entirely employed in giving names to things, and not in searching into things themselves, we may say that they have invented a philosophical way of speaking, but not that they have made known to us true philosophy.

Others therefore by laying aside that useless heap of words, thought to employ their pains to better purpose. These supposed all matter homogeneous, and that the variety of forms which is seen in bodies arises from some very plain and simple affections of the component particles. And by going on from simple things to those which are more compounded they certainly proceed right; if they attribute no other properties to those primary affections of the particles than Nature has done. But when they take a liberty of imagining at pleasure unknown figures and magnitudes, and uncertain situations and motions of the parts; and moreover of supposing occult fluids, freely pervading the pores of bodies, endued with an all-performing subtilty, and agitated with occult motions; they now run out into dreams and chimera's, and neglect the true constitution of things; which certainly is not to be expected from fallacious conjectures, when we can scarce reach it by the most certain observations. Those who fetch from hypotheses the foundation on which they build their speculations, may form indeed an ingenious romance, but a romance it will still be.

There is left then the third class, which professes experimental philosophy. These indeed derive the causes of all things from the most simple principles possible;

### Mr. COTES'S PREFACE.

possible; but then they assume nothing as a principle, that is not proved by phenomena. They frame no hypotheses, nor receive them into philosophy otherwise than as questions whose truth may be disputed. They proceed therefore in a twofold method, synthetical and analytical. From some select phenomena they deduce by analysis the forces of nature, and the more simple laws of forces; and from thence by synthesis shew the constitution of the rest. This is that incomparably best way of philosophizing, which our renowned author most justly embraced before the rest; and thought alone worthy to be cultivated and adorned by his excellent labours. Of this he has given us a most illustrious example, by the explication of the System of the

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